Exercise 46

Zoom in toward the points (1,0), (0,1), and (-1,0) on the graph of the function $g(x) = (x^2 - 1)^{2/3}$. What do you notice? Account for what you see in terms of the differentiability of g.

Solution

Below is a graph of g(x) versus x.



Zoom in towards the point (-1,0). Notice that no matter how much you zoom in, the graph never becomes a straight line.





Now zoom in towards the point (0, 1). Notice that the graph is practically a straight line.

Zoom in towards the point (1,0). Notice that no matter how much you zoom in, the graph never becomes a straight line.

